

UNIVERSITI KUALA LUMPUR
BUSINESS SCHOOL

FINAL EXAMINATION
MARCH 2026 SEMESTER

COURSE CODE : EAB11603
COURSE TITLE : STATISTICS FOR ACCOUNTING
PROGRAMME NAME : BACHELOR OF SCIENCE (HONOURS) IN ANALYTICAL
ECONOMICS
DATE : 27 JUNE 2026
TIME : 9:00AM - 12:00PM
DURATION : 3 HOURS

INSTRUCTIONS TO CANDIDATES

1. Please read the instructions given in the question paper CAREFULLY.
2. This question paper is printed on both sides of the paper.
3. This question paper consist of ONE sections.
4. Section A consist of five questions. Answer FOUR (4) questions only.
5. Please write your answer on the answer booklet provided.
6. Please answer all questions in English only.
7. Refer to the attached Formula/ Appendies. ☐ Tick if applicable

THERE ARE 13 PAGES OF QUESTIONS INCLUDING THIS PAGE

SECTION A (Total: 100 marks)

Answer FOUR (4) questions.

Please use the answer booklet provided.

Question 1

Answer all questions below.

- (a) A large accounting firm reports that the average time required to complete an individual tax audit is 20 hours, with a population standard deviation of 5 hours. A senior audit manager randomly selects 66 completed tax audit cases to evaluate the efficiency of the audit department. Based on this information:
- Calculate the probability that the sample mean audit completion time exceeds 18.5 hours.
(3 marks)
 - Determine the probability that the sample mean completion time lies between 19.8 and 21.5 hours.
(4 marks)
- (b) A retail analytics company in Malaysia is analyzing whether there is a difference in the average amount spent per transaction between customers shopping during weekday promotional campaigns and customers shopping during weekend promotional campaigns, as marketing strategies are being evaluated to maximize sales performance. A random sample of 27 weekday promotional shoppers recorded an average spending of RM85 with a sample standard deviation of RM18, while a random sample of 29 weekend promotional shoppers recorded an average spending of RM97 with a sample standard deviation of RM21. Construct a 99% confidence interval for the difference between the two population mean transaction amounts.
Refer Below - Table1 : . .
(6 marks)

Table 1: .

$n_1 = 27$	$n_2 = 29$
$\bar{x}_1 = 85$	$\bar{x}_2 = 97$
$s_1 = 18$	$s_2 = 21$

- (c) The internal audit department of Petronas is investigating whether there is a significant relationship between employee department and the occurrence of accounting errors detected during annual financial audits after the company implemented a new computerized accounting information system. Employees were classified according to four departments — Finance, Purchasing, Human Resource, and Operations — while audit findings were categorized into three types of accounting errors: Documentation Errors, Calculation Errors, and Reporting Errors. The audit manager collected data from 400 audit cases across multiple branches, and accounting students are required to apply the chi-square test of independence at the 5% significance level to determine whether department type is associated with the type of accounting errors identified during the audit process.

Department	Documentation Errors	Calculation Error	Reporting Errors	Total
Finance	28	35	17	80
Purchasing	42	31	27	100
HR	25	18	22	65
Operations	55	46	54	155
Total	150	130	120	400

Calculate the expected frequency.

(4 marks)

- (d) A university researcher wants to study the relationship between the number of hours students spend playing video games each week and their cumulative grade point averages (CGPA), because excessive gaming may influence academic performance. The following data in the table below are collected from seven students. Compute the correlation coefficient and interpret your answer.

Refer Below - Table2 : . .

(5 marks)

Table 2: .

Video Game Hours per Week (x)	CGPA (y)
2	3.82
4	3.65
6	3.42
8	3.21
10	3.05
12	2.88
15	2.60

- (e) The cost accounting department of Petronas is conducting a detailed inflation analysis to evaluate how changes in key production input costs have affected overall manufacturing expenses between 2024 (base year) and 2025 (current year). The finance manager is particularly interested in comparing different index number methods — Laspeyres, Paasche, and Fisher's Ideal Index — to determine the most accurate measure of cost inflation in the production process. Three major inputs are considered: raw materials, labour hours, and energy consumption, and both price and quantity data for the two years have been collected for analysis by accounting students.

Input	2024		2025	
	Price (RM)	Quantity	Price (RM)	Quantity
Raw Materials	50	100	65	120
Labour Hours	40	80	48	90
Energy	30	60	36	70

Calculate the Laspeyres Quantity Index.

(3 marks)

Question 2

Answer all questions below.

- (a) An automotive engineer wants to estimate the cost of repairing a car that experiences a 25 MPH head-on collision. He crashes 24 cars, and the average repair is \$11,000. The standard deviation of the 24-cars is \$2,500. Provide a 95% confidence interval for the true mean cost of repair.

(4 marks)

- (b) A cinema company claims that customers spend an average of 2.5 hours at its movie theaters, including time spent watching movies and purchasing refreshments. A business analyst believes that the average time has increased because more customers are attending extended premium screenings. A random sample of 27 customers shows an average stay of 2.9 hours with a sample standard deviation of 0.7 hours. Using a significance level of 0.05, test whether there is sufficient evidence to support the analyst's belief.

- i. State the hypothesis.

(1 marks)

- ii. Calculate the test statistic.

(2 marks)

- iii. Make your decision and interpret your answer.

(2 marks)

- (c) The internal audit division of Maybank is conducting a study to determine whether there is a relationship between branch location and types of internal control weaknesses detected during audits after a system upgrade. Branches are grouped into four regions — Central, Northern, Southern, and East Coast — while weaknesses are classified into three categories: Cash Handling Errors, Authorization Errors, and System Entry Errors. Data from 480 audit findings were collected, and students are required to apply a chi-square test of independence at the 5% significance level.

Region	Cash Handling	Authorization	System Entry	Total
Central	38	42	40	120
Northern	30	35	35	100
Southern	45	40	35	120
East Coast	32	40	68	140
Total	145	157	178	480

Find the expected value.

(4 marks)

- (d) A manufacturing engineer wants to examine the relationship between the number of hours a machine operates continuously and the amount of energy consumed during production, because understanding energy usage patterns may help reduce operating costs. Data from six production days are given below:

Refer Below - Table3 : . .

Table 3: .

Machine Operating Hours (x)	Energy Consumption (kWh) (y)
3	120
5	165
6	190
8	245
10	295
12	360

- i. Draw a scatter diagram. (3 marks)
 - ii. Compute the correlation coefficient, r . (5 marks)
 - iii. Interpret the relationship between x and y . (1 marks)
- (e) The finance department of is analyzing whether revenue from different ticket classes has changed significantly over time due to changes in pricing strategy and demand patterns. The company compares 2023 (base year) and 2025 (current year) using index numbers.

Ticket Class	2023		2025	
	Price (RM)	Quantity	Price (RM)	Quantity
Economy	200	500	250	600
Premium Economy	400	200	450	220
Business	800	100	900	120

Calculate the Paasche Quantity Index.

(3 marks)

Question 3

Answer all questions below.

- (a) A public accounting firm reports that 90% of its audit engagements are completed within the scheduled audit timeline agreed upon with clients. A quality-control reviewer randomly selects 100 completed audit projects to evaluate audit efficiency. Determine the probability that the sample proportion lies between 0.86 and 0.92.

(5 marks)

- (b) A sports scientist is comparing the average sprint completion times of athletes following two different training programs. A random sample of 14 athletes using Training Program A records an average sprint time of 11.8 seconds with a sample standard deviation of 0.6 seconds, while a random sample of 15 athletes using Training Program B records an average sprint time of 12.3 seconds with a sample standard deviation of 0.7 seconds. At the 5% significance level, determine whether there is enough evidence to conclude that the mean sprint times differ between the two training programs.

Refer Below - Table4 : . .

(6 marks)

Table 4: .

Training Program A	Training Program B
$n_1 = 14$	$n_2 = 15$
$x_1 = 11.8$	$x_2 = 12.3$
$s_1 = 0.6$	$s_2 = 0.7$

- (c) A manufacturing company wants to determine whether inventory discrepancy occurrence is associated with warehouse location. An internal audit is conducted, and the following results are obtained.

Refer Below - Table5 : . .

Table 5: .

Warehouse Location	Inventory Discrepancy Found	No Discrepancy Found	Total
North Region	52	148	200
Central Region	37	163	200
South Region	61	139	200
Total	150	450	600

i. Formulate the hypotheses.

(1 marks)

ii. Compute the expected frequencies.

(4 marks)

- (d) A logistics company wants to study the relationship between delivery distance and fuel costs for transportation vehicles, because understanding fuel expenses is important for planning and budgeting operations. The following data are collected from seven delivery trips. Find the least squares regression line.

Refer Below - Table6 : . .

(4 marks)

Table 6: .

Delivery Distance (x)	Fuel Cost (y)
20	18
35	27
50	36
65	47
80	56
95	68
110	79

- (e) The audit and assurance department of PwC is analyzing whether the cost of audit operations has increased significantly over time due to higher manpower costs, software usage, and travel expenses incurred during audit engagements, and the finance manager wants to evaluate overall cost inflation between 2024 and 2025 for budgeting and billing purposes.

Cost Item	2024		2025	
	Price (RM)	Quantity	Price (RM)	Quantity
Manpower	400	50	480	55
Software Tools	200	80	260	90
Travel Expenses	150	60	180	70

Calculate the LPI and PPI.

(5 marks)

Question 4

Answer all questions below.

- (a) A retail company wants to estimate the proportion of branch managers who submit monthly financial reports on time to the head office. A financial controller randomly selects 200 branch reports and finds that 168 reports were submitted before the reporting deadline. Using a 90% confidence level, construct the confidence interval for the true proportion of managers submitting reports on time.

(4 marks)

- (b) A tech company is testing two different server configuration to determine which provides faster website loading times and follows normal distribution. Based on prior testing, the population standard deviation for Configuration A is known to be 0.8 seconds and for Configuration B is 1.0 second. A sample of 40 loading times using Configuration A has an average of 3.2 seconds. A sample of 36 loading times using Configuration B has an average of 3.6 seconds. At 5% level of significance:

- i. State the hypotheses to test whether Configuration A has a lower mean loading time than Configuration B.

(1 marks)

- ii. Calculate the test statistic.

(3 marks)

- iii. Determine the rejection region. Make a decision whether to reject or fail to reject the hypothesis.

(3 marks)

- (c) A company's payroll division wants to determine whether overtime approval status is associated with employee department. A random sample of payroll records is selected, and the following information including the expected frequencies are obtained. Calculate the Chi Square test statistic.

Refer Below - Table7 : . .

(5 marks)

Table 7: .

Department	Overtime Approved	Overtime Rejected	Total
Finance	73 (69.55)	17 (20.45)	90
Operations	94 (100.45)	36 (29.55)	130
Sales	88 (85)	22 (25)	110
Total	255	75	330

- (d) A logistic manager is trying to understand how the distance between a warehouse and delivery location affects the total delivery time. Below are the data after collecting data from several deliveries under normal traffic conditions. Calculate the regression equation.

Refer Below - Table8 : . .

(4 marks)

Table 8: .

Distance (km)	Delivery Time (minutes)
5	15
10	22
15	30
20	36
25	50
30	65

- (e) The audit and assurance department of PwC is analyzing whether the cost of audit operations has increased significantly over time due to higher manpower costs, software usage, and travel expenses incurred during audit engagements, and the finance manager wants to evaluate overall cost inflation between 2024 and 2025 for budgeting and billing purposes.

Cost Item	2024		2025	
	Price (RM)	Quantity	Price (RM)	Quantity
Manpower	400	50	480	55
Software Tools	200	80	260	90
Travel Expenses	150	60	180	70

Find the Fisher Quantity Index.

(5 marks)

Question 5

Answer all questions below.

- (a) A hotel company reports that the average monthly maintenance expense for its hotels is RM92,000, with a population standard deviation of RM11,500. A company accountant randomly selects 81 months of maintenance expense records to evaluate expense stability. Determine the probability that the sample mean maintenance expense lies between RM90,500 and RM93,000.

(5 marks)

- (b) A sample of 15 final-year students were found to spend on average 15 hours per week in the university library, with a standard deviation 3 hours. A sample of 20 freshers found they spend on average 9 hours per week in the library, with a standard deviation 5 hours. Using a significance level 0.05, is there a sufficient evidence to conclude that final-year students spend more time in the library than the fresher students?

(9 marks)

- (c) The internal audit department of IBM is evaluating whether different training methods for accounting staff affect the average number of accounting errors detected per month. Three training methods were used: Online Training, Classroom Training, and Hybrid Training. Data were collected from five months.

Month	Online	Classroom	Hybrid
1	8	6	4
2	7	5	3
3	9	6	4
4	8	7	5
5	7	6	4

$$H_0: \mu_1 = \mu_2 = \mu_3$$

H_1 : At least one training method has a different mean number of errors.

$$\alpha = 0.05$$

	SS	df	Mean Squares	F value
Treatment	36.13	2	18.07	31.07
Error	6.8	12	0.57	
Total	42.93	14		

Find the critical value and make decision to reject or fail to reject the null hypothesis. Interpret.

(3 marks)

- (d) There has been much focused on measuring happiness in recent years. The data below are derived from the World Happiness Report¹⁰ and measure average happiness (on a scale of 1-10, obtained from a survey of citizens) and the logarithm of GDP per capita (in US \$000) for a subset of countries. These problems ask you to explore the relationship between them. Find the correlation coefficient between happiness and $\ln_gdp$. Interpret the value.

Refer Below - Table9 : . .

(5 marks)

Table 9: .

Country	Happiness	$\ln_gdp$
Austria	7.1	10.9
Bulgaria	5.4	10.1
Italy	6.5	10.6
Sweden	7.4	10.9
United Kingdom	6.9	10.7

- (e) The audit operations division of is analyzing whether the workload of audit teams has increased due to stricter regulatory requirements, and the firm tracks workload in terms of audit hours, client visits, and documentation tasks across two years, requiring students to compute quantity index numbers for performance evaluation.

Activity	Price (RM)		Quantity	
	2022	2025	2022	2025
Audit Hours	300	350	120	150
Client Visits	200	240	100	120
Documentation Tasks	150	180	80	90

Calculate the PPI.

(3 marks)

END OF EXAMINATION PAPER

FORMULAS AND STATISTICAL TABLE

PROBABILITY DISTRIBUTIONS

Normal distribution:

$$Z = \frac{X - \mu}{\sigma}$$

Standard error of the mean:

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}, \sigma_{\bar{p}} = \sqrt{\frac{pq}{n}}$$

SAMPLING ESTIMATIONS

Sample mean:

$$\bar{x} = \frac{\sum x}{n}$$

Margin of error:

$$E = Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

Sample standard deviation:

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}} @ s = \sqrt{\frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n-1}}$$

$$E = t_{\alpha/2} \frac{s}{\sqrt{n}}$$

$$E = Z_{\alpha/2} \sqrt{\frac{\bar{p}(1-\bar{p})}{n}}$$

Sample proportion:

$$\hat{p} = \frac{x}{n}$$

Confidence interval (one population):

$$CI = \bar{x} \pm Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$CI = \bar{x} \pm t_{\alpha/2, df} \left(\frac{s}{\sqrt{n}} \right) \text{ where } df = n-1$$

Sample size:

$$n = \left(\frac{Z\sigma}{E} \right)^2$$

$$n = \frac{(Z)^2 pq}{E^2}$$

$$CI = \bar{p} \pm Z_{\alpha/2} \sqrt{\frac{\bar{p}(1-\bar{p})}{n}}$$

Confidence interval (two populations):

$$CI = (\bar{x}_1 - \bar{x}_2) \pm Z_{\alpha/2} \left(\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \right)$$

$$CI = (\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2} \left(\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} \right)$$

$$\text{where, } df = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2} \right)^2}{\frac{1}{n_1-1} \left(\frac{s_1^2}{n_1} \right)^2 + \frac{1}{n_2-1} \left(\frac{s_2^2}{n_2} \right)^2}$$

Sampling distribution:

$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

$$t = \frac{\bar{x} - \mu}{s / \sqrt{n}}$$

$$Z = \frac{\bar{p} - p_0}{\sqrt{\frac{pq}{n}}}$$

$$CI = (\hat{p}_1 - \hat{p}_2) \pm Z_{\alpha/2} \left(\sqrt{\frac{\hat{p}_1 \hat{q}_1}{n_1} + \frac{\hat{p}_2 \hat{q}_2}{n_2}} \right)$$

HYPOTHESIS TESTING AND DISTRIBUTIONS

Test statistic:

$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

$$Z = \frac{\bar{p} - p_0}{\sigma_{\bar{p}}}$$

$$t = \frac{\bar{x} - \mu}{s / \sqrt{n}}$$

$$Z = \frac{p_1 - p_2}{\sqrt{\bar{p}\bar{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$$

Pooled estimator:

$$\bar{p} = \frac{p_1 n_1 + p_2 n_2}{n_1 + n_2}$$

HYPOTHESIS TESTING TWO POPULATIONS

$$Z = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

$$Z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\bar{p}\bar{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$$

$$t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$$df = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}\right)^2}{\frac{1}{n_1 - 1} \left(\frac{s_1^2}{n_1}\right)^2 + \frac{1}{n_2 - 1} \left(\frac{s_2^2}{n_2}\right)^2}$$

Chi-square:

$$\chi^2 = \sum \frac{(O - E)^2}{E}$$

$$df = (c - 1)(r - 1)$$

Anova:

$$F = \frac{s_1^2}{s_2^2}, F = \frac{MST}{MSE}$$

$$MST = \frac{SST}{k - 1}$$

$$MSE = \frac{SSE}{n - k}$$

$$SST = SST_{total} - SSE$$

Degrees of freedom in the numerator:

$$df = k - 1,$$

 k = number of treatments

Degrees of freedom in the denominator:

$$df = n - k,$$

 n = number of observations k = number of treatments

REGRESSION AND CORRELATION

$$r = \frac{n(\sum xy) - (\sum x)(\sum y)}{\sqrt{[n\sum x^2 - (\sum x)^2][n\sum y^2 - (\sum y)^2]}}$$

$$a = \frac{[(\sum y)(\sum x^2) - (\sum x)(\sum xy)]}{[n(\sum x^2) - (\sum x)^2]}$$

Regression line equation:

$$y = a + bx$$

$$b = \frac{[n(\sum xy) - (\sum x)(\sum y)]}{[n(\sum x^2) - (\sum x)^2]}$$

INDEX NUMBER

Simple Index Number:

$$P_I = \frac{p_i}{p_0} \times 100$$

Paasche Index:

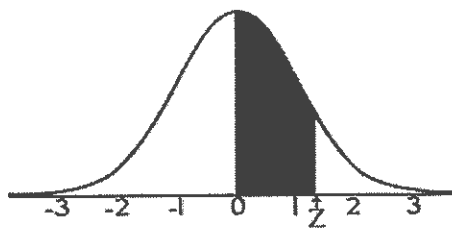
$$P_P^n = \frac{\sum p_n q_n}{\sum p_0 q_n} \times 100$$

Laspeyres Index:

$$P_L^n = \frac{\sum p_n q_0}{\sum p_0 q_0} \times 100$$

Fisher Price Index:

$$FPI = (\text{Laspeyres Index} \times \text{Paasche Index})^{0.5}$$

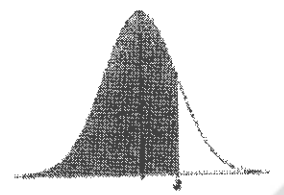


STANDARD NORMAL TABLE (z)

Entries in the table give the area under the curve between the mean and z standard deviations above the mean. For example, for $z = 1.25$ the area under the curve between the mean (0) and z is 0.3944.

	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0190	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2969	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3513	0.3554	0.3577	0.3529	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
3.1	0.4990	0.4991	0.4991	0.4991	0.4992	0.4992	0.4992	0.4992	0.4993	0.4993
3.2	0.4993	0.4993	0.4994	0.4994	0.4994	0.4994	0.4994	0.4995	0.4995	0.4995
3.3	0.4995	0.4995	0.4995	0.4996	0.4996	0.4996	0.4996	0.4996	0.4996	0.4997
3.4	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4998

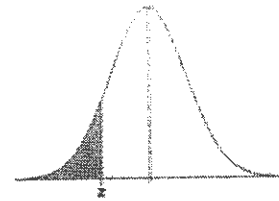
Standard Normal Cumulative Probability Table



Cumulative probabilities for POSITIVE z-values are shown in the following table:

z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998

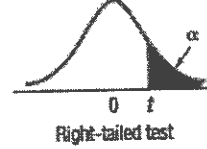
Standard Normal Cumulative Probability Table



Cumulative probabilities for NEGATIVE z-values are shown in the following table:

z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
-3.4	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0002
-3.3	0.0005	0.0005	0.0005	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004	0.0003
-3.2	0.0007	0.0007	0.0006	0.0006	0.0006	0.0006	0.0006	0.0006	0.0005	0.0005
-3.1	0.0010	0.0009	0.0009	0.0009	0.0008	0.0008	0.0008	0.0008	0.0007	0.0007
-3.0	0.0013	0.0013	0.0013	0.0012	0.0012	0.0011	0.0011	0.0011	0.0010	0.0010
-2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
-2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
-2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
-2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
-2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
-2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
-2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
-2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
-2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
-2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
-1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
-1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
-1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
-1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
-1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
-1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
-1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
-1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
-1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
-1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
-0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
-0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
-0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
-0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
-0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
-0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
-0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
-0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
-0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641

B.5 Student's *t* Distribution



Confidence Intervals, <i>c</i>						
<i>df</i>	80%	90%	95%	98%	99%	99.9%
	Level of Significance for One-Tailed Test, α					
	0.10	0.05	0.025	0.01	0.005	0.0005
	Level of Significance for Two-Tailed Test, α					
	0.20	0.10	0.05	0.02	0.01	0.001
1	3.078	6.314	12.706	31.821	63.657	636.619
2	1.886	2.920	4.303	6.985	9.925	31.599
3	1.638	2.353	3.182	4.541	5.841	12.924
4	1.533	2.132	2.778	3.747	4.604	8.610
5	1.476	2.015	2.571	3.365	4.032	6.869
6	1.440	1.943	2.447	3.143	3.707	5.959
7	1.415	1.895	2.365	2.998	3.499	5.408
8	1.397	1.860	2.306	2.898	3.355	5.041
9	1.383	1.833	2.262	2.821	3.250	4.781
10	1.372	1.812	2.228	2.764	3.169	4.587
11	1.363	1.796	2.201	2.718	3.106	4.437
12	1.356	1.782	2.179	2.681	3.055	4.318
13	1.350	1.771	2.160	2.650	3.012	4.221
14	1.345	1.761	2.145	2.624	2.977	4.140
15	1.341	1.753	2.131	2.602	2.947	4.073
16	1.337	1.746	2.120	2.583	2.921	4.015
17	1.333	1.740	2.110	2.567	2.898	3.965
18	1.330	1.734	2.101	2.552	2.878	3.922
19	1.328	1.729	2.093	2.539	2.861	3.883
20	1.325	1.725	2.086	2.528	2.845	3.850
21	1.323	1.721	2.080	2.518	2.831	3.819
22	1.321	1.717	2.074	2.508	2.819	3.792
23	1.319	1.714	2.069	2.500	2.807	3.768
24	1.318	1.711	2.064	2.492	2.797	3.745
25	1.316	1.708	2.060	2.485	2.787	3.725
26	1.315	1.706	2.056	2.479	2.779	3.707
27	1.314	1.703	2.052	2.473	2.771	3.690
28	1.313	1.701	2.048	2.467	2.763	3.674
29	1.311	1.699	2.045	2.462	2.756	3.659
30	1.310	1.697	2.042	2.457	2.750	3.646
31	1.309	1.696	2.040	2.453	2.744	3.633
32	1.309	1.694	2.037	2.449	2.738	3.622
33	1.308	1.692	2.035	2.445	2.733	3.611
34	1.307	1.691	2.032	2.441	2.728	3.601
35	1.306	1.690	2.030	2.438	2.724	3.591

Confidence Intervals, <i>c</i>						
<i>df</i>	80%	90%	95%	98%	99%	99.9%
	Level of Significance for One-Tailed Test, α					
	0.10	0.05	0.025	0.01	0.005	0.0005
	Level of Significance for Two-Tailed Test, α					
	0.20	0.10	0.05	0.02	0.01	0.001
36	1.306	1.686	2.028	2.434	2.719	3.582
37	1.305	1.687	2.026	2.431	2.715	3.574
38	1.304	1.686	2.024	2.429	2.712	3.566
39	1.304	1.685	2.022	2.426	2.708	3.558
40	1.303	1.684	2.021	2.423	2.704	3.551
41	1.303	1.683	2.020	2.421	2.701	3.544
42	1.302	1.682	2.018	2.418	2.699	3.538
43	1.302	1.681	2.017	2.416	2.695	3.532
44	1.301	1.680	2.015	2.414	2.692	3.526
45	1.301	1.679	2.014	2.412	2.690	3.520
46	1.300	1.679	2.013	2.410	2.687	3.515
47	1.300	1.678	2.012	2.408	2.685	3.510
48	1.299	1.677	2.011	2.407	2.682	3.505
49	1.299	1.677	2.010	2.405	2.680	3.500
50	1.299	1.676	2.009	2.403	2.678	3.496
51	1.298	1.675	2.008	2.402	2.676	3.492
52	1.298	1.675	2.007	2.400	2.674	3.488
53	1.298	1.674	2.006	2.399	2.672	3.484
54	1.297	1.674	2.005	2.397	2.670	3.480
55	1.297	1.673	2.004	2.396	2.668	3.476
56	1.297	1.673	2.003	2.395	2.667	3.473
57	1.297	1.672	2.002	2.394	2.665	3.470
58	1.296	1.672	2.002	2.392	2.663	3.466
59	1.296	1.671	2.001	2.391	2.662	3.463
60	1.296	1.671	2.000	2.390	2.660	3.460
61	1.296	1.670	2.000	2.389	2.659	3.457
62	1.295	1.670	1.999	2.388	2.657	3.454
63	1.295	1.669	1.998	2.387	2.656	3.452
64	1.295	1.669	1.998	2.386	2.655	3.449
65	1.295	1.669	1.997	2.385	2.654	3.447
66	1.295	1.668	1.997	2.384	2.652	3.444
67	1.294	1.668	1.996	2.383	2.651	3.442
68	1.294	1.668	1.995	2.382	2.650	3.439
69	1.294	1.667	1.995	2.382	2.649	3.437
70	1.294	1.667	1.994	2.381	2.648	3.435

(continued)

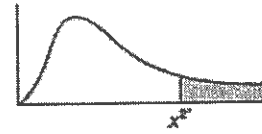
B.5 Student's *t* Distribution (*concluded*)

df	Confidence Intervals, <i>c</i>					
	80%	90%	95%	98%	99%	99.9%
	Level of Significance for One-Tailed Test, α					
	0.10	0.05	0.025	0.01	0.005	0.0005
	Level of Significance for Two-Tailed Test, α					
	0.20	0.10	0.05	0.02	0.01	0.001
71	1.294	1.667	1.994	2.380	2.647	3.433
72	1.293	1.666	1.993	2.379	2.646	3.431
73	1.293	1.666	1.993	2.379	2.645	3.429
74	1.293	1.666	1.993	2.378	2.644	3.427
75	1.293	1.665	1.992	2.377	2.643	3.425
76	1.293	1.665	1.992	2.376	2.642	3.423
77	1.293	1.665	1.991	2.376	2.641	3.421
78	1.292	1.665	1.991	2.375	2.640	3.420
79	1.292	1.664	1.990	2.374	2.640	3.418
80	1.292	1.664	1.990	2.374	2.639	3.416
81	1.292	1.664	1.990	2.373	2.638	3.415
82	1.292	1.664	1.989	2.373	2.637	3.413
83	1.292	1.663	1.989	2.372	2.636	3.412
84	1.292	1.663	1.989	2.372	2.636	3.410
85	1.292	1.663	1.988	2.371	2.635	3.408
86	1.291	1.663	1.988	2.370	2.634	3.407
87	1.291	1.663	1.988	2.370	2.634	3.406
88	1.291	1.662	1.987	2.369	2.633	3.405

df	Confidence Intervals, <i>c</i>					
	80%	90%	95%	98%	99%	99.9%
	Level of Significance for One-Tailed Test, α					
	0.10	0.05	0.025	0.01	0.005	0.0005
	Level of Significance for Two-Tailed Test, α					
	0.20	0.10	0.05	0.02	0.01	0.001
89	1.291	1.662	1.987	2.369	2.632	3.403
90	1.291	1.662	1.987	2.368	2.632	3.402
91	1.291	1.662	1.986	2.368	2.631	3.401
92	1.291	1.662	1.986	2.368	2.630	3.399
93	1.291	1.661	1.986	2.367	2.630	3.398
94	1.291	1.661	1.986	2.367	2.629	3.397
95	1.291	1.661	1.985	2.366	2.629	3.396
96	1.290	1.661	1.985	2.366	2.628	3.395
97	1.290	1.661	1.985	2.365	2.627	3.394
98	1.290	1.661	1.984	2.365	2.627	3.393
99	1.290	1.660	1.984	2.365	2.626	3.392
100	1.290	1.660	1.984	2.364	2.626	3.390
120	1.289	1.658	1.980	2.358	2.617	3.373
140	1.288	1.656	1.977	2.353	2.611	3.361
160	1.287	1.654	1.975	2.350	2.607	3.352
180	1.286	1.653	1.973	2.347	2.603	3.345
200	1.286	1.653	1.972	2.345	2.601	3.340
∞	1.282	1.645	1.960	2.326	2.576	3.291

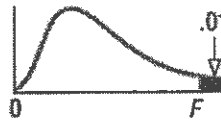
Table A4 Critical values of the χ^2 distribution

The values in the table give the critical values of χ^2 which cut off the area in the right-hand tail given at the top of the column.



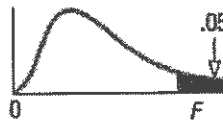
v	Area in right-hand tail						
	0.995	0.990	0.975	0.950	0.900	0.750	0.500
1	392704.10 ⁻¹⁰	157088.10 ⁻⁹	982069.10 ⁻⁹	393214.10 ⁻⁸	0.0157908	0.1015308	0.454936
2	0.0100251	0.0201007	0.0506356	0.102587	0.210721	0.575364	1.38629
3	0.0717218	0.114832	0.215795	0.351846	0.584374	1.212534	2.36597
4	0.206989	0.297109	0.484419	0.710723	1.063623	1.92256	3.35669
5	0.411742	0.554298	0.831212	1.145476	1.61031	2.67460	4.35146
6	0.675727	0.872090	1.23734	1.63538	2.20413	3.45460	5.34812
7	0.989256	1.239043	1.68987	2.16735	2.83311	4.25485	6.34581
8	1.34441	1.64650	2.17973	2.73264	3.48954	5.07064	7.34412
9	1.73493	2.08790	2.70039	3.32511	4.16816	5.89883	8.34283
10	2.15586	2.55821	3.24697	3.94030	4.86518	6.73720	9.34182
11	2.60322	3.05348	3.81575	4.57481	5.57778	7.58414	10.3410
12	3.07382	3.57057	4.40379	5.22603	6.30380	8.43842	11.3403
13	3.56503	4.10692	5.00875	5.89186	7.04150	9.29907	12.3398
14	4.07467	4.66043	5.62873	6.57063	7.78953	10.1653	13.3393
15	4.60092	5.22935	6.26214	7.26094	8.54676	11.0365	14.3389
16	5.14221	5.81221	6.90766	7.96165	9.31224	11.9122	15.3385
17	5.69722	6.40776	7.56419	8.67176	10.0852	12.7919	16.3382
18	6.26480	7.01491	8.23075	9.39046	10.8649	13.6753	17.3379
19	6.84397	7.63273	8.90652	10.1170	11.6509	14.5620	18.3377
20	7.43384	8.26040	9.59078	10.8508	12.4426	15.4518	19.3374
21	8.03365	8.89720	10.28293	11.5913	13.2396	16.3444	20.3372
22	8.64272	9.54249	10.9823	12.3380	14.0415	17.2396	21.3370
23	9.26043	10.19567	11.6886	13.0905	14.8480	18.1373	22.3369
24	9.88623	10.8564	12.4012	13.8484	15.6587	19.0373	23.3367
25	10.5197	11.5240	13.1197	14.6114	16.4734	19.9393	24.3366
26	11.1602	12.1981	13.8439	15.3792	17.2919	20.8434	25.3365
27	11.8076	12.8785	14.5734	16.1514	18.1139	21.7494	26.3363
28	12.4613	13.5647	15.3079	16.9279	18.9392	22.6572	27.3362
29	13.1211	14.2565	16.0471	17.7084	19.7677	23.5666	28.3361
30	13.7867	14.9535	16.7908	18.4927	20.5992	24.4776	29.3360
40	20.7065	22.1643	24.4330	26.5093	29.0505	33.6603	39.3353
50	27.9907	29.7067	32.3574	34.7643	37.6886	42.9421	49.3349
60	35.5345	37.4849	40.4817	43.1880	46.4589	52.2938	59.3347
70	43.2752	45.4417	48.7576	51.7393	55.3289	61.6983	69.3345
80	51.1719	53.5401	57.1532	60.3915	64.2778	71.1445	79.3343
90	59.1963	61.7541	65.6466	69.1260	73.2911	80.6247	89.3342
100	67.3276	70.0649	74.2219	77.9295	82.3581	90.1332	99.3341

v	0.250	0.100	0.050	0.025	0.010	0.005	0.001
1	1.32330	2.70554	003.84146	5.02389	6.63490	7.87944	10.828
2	2.77259	4.60517	5.99146	7.37776	9.21034	10.5966	13.816
3	4.10834	6.25139	7.81473	9.34840	11.3449	12.8362	16.266
4	5.38527	7.77944	9.48773	11.1433	13.2767	14.8603	18.467
5	6.62568	9.23636	11.0705	12.8325	15.0863	16.7496	20.515
6	7.84080	10.6446	12.5916	14.4494	16.8119	18.5476	22.458
7	9.03715	12.0170	14.0671	16.0128	18.4753	20.2777	24.322
8	10.2189	13.3616	15.5073	17.5345	20.0902	21.9550	26.125
9	11.3888	14.6837	16.9190	19.0228	21.6660	23.5894	27.877
10	12.5489	15.9872	18.3070	20.4832	23.2093	25.1882	29.588
11	13.7007	17.2750	19.6751	21.9200	24.7250	26.7568	31.264
12	14.8454	18.5493	21.0261	23.3367	26.2170	28.2995	32.909
13	15.9839	19.8119	22.3620	24.7356	27.6882	29.8195	34.528
14	17.1169	21.0641	23.6848	26.1189	29.1412	31.3194	36.123
15	18.2451	22.3071	24.9958	27.4884	30.5779	32.8013	37.697
16	19.3689	23.5418	26.2962	28.8454	31.9999	34.2672	39.252
17	20.4887	24.7690	27.5871	30.1910	33.4087	35.7185	40.790
18	21.6049	25.9894	28.8693	31.5264	34.8053	37.1565	42.312
19	22.7178	27.2036	30.1435	32.8523	36.1909	38.5823	43.820
20	23.8277	28.4120	31.4104	34.1696	37.5662	39.9968	45.315
21	24.9348	29.6151	32.6706	35.4789	38.9322	41.4011	46.797
22	26.0403	30.8133	33.9244	36.7807	40.2894	42.7957	48.268
23	27.1413	32.0069	35.1725	38.0756	41.6384	44.1813	49.728
24	28.2412	33.1962	36.4150	39.3641	42.9798	45.5585	51.179
25	29.3389	34.3816	37.6525	40.6465	44.3141	46.9279	52.618
26	30.4346	35.5632	38.8851	41.9232	45.6417	48.2899	54.052
27	31.5284	36.7412	40.1133	43.1945	46.9629	49.6449	55.476
28	32.6205	37.9150	41.3371	44.4608	48.2782	50.9934	56.892
29	33.7109	39.0875	42.5570	45.7223	49.5879	52.3356	58.301
30	34.7997	40.2560	43.7730	46.9792	50.8922	53.6720	59.703
40	45.6160	51.8051	55.7585	59.3417	63.6907	66.7660	73.402
50	56.3336	63.1671	67.5048	71.4202	76.1539	79.4900	86.661
60	66.9815	74.3970	79.0819	83.2977	88.3794	91.9517	99.607
70	77.5767	85.5270	90.5312	95.0232	100.425	104.215	112.317
80	88.1303	96.5782	101.879	106.629	112.329	116.321	124.839
90	98.6499	107.565	113.145	118.136	124.116	128.299	137.208
100	109.141	118.498	124.342	129.561	135.807	140.169	149.449

B.6B Critical Values of the F Distribution ($\alpha = .01$)

		Degrees of Freedom for the Numerator															
		1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40
Degrees of Freedom for the Denominator	1	4052	5000	5403	5625	5764	5859	5928	5981	6022	6056	6106	6157	6209	6235	6261	6287
	2	98.5	99.0	99.2	99.2	99.3	99.3	99.4	99.4	99.4	99.4	99.4	99.4	99.4	99.5	99.5	99.5
	3	34.1	30.8	29.5	28.7	28.2	27.9	27.7	27.5	27.3	27.2	27.1	26.9	26.7	26.6	26.5	26.4
	4	21.2	18.0	16.7	16.0	15.5	15.2	15.0	14.8	14.7	14.5	14.4	14.2	14.0	13.9	13.8	13.7
	5	16.3	13.3	12.1	11.4	11.0	10.7	10.5	10.3	10.2	10.1	9.89	9.72	9.55	9.47	9.38	9.29
	6	13.7	10.9	9.78	9.15	8.75	8.47	8.26	8.10	7.98	7.87	7.72	7.56	7.40	7.31	7.23	7.14
	7	12.2	9.55	8.45	7.85	7.46	7.19	6.99	6.84	6.72	6.62	6.47	6.31	6.16	6.07	5.99	5.91
	8	11.3	8.65	7.59	7.01	6.63	6.37	6.18	6.03	5.91	5.81	5.67	5.52	5.36	5.28	5.20	5.12
	9	10.6	8.02	6.99	6.42	6.06	5.80	5.61	5.47	5.35	5.26	5.11	4.96	4.81	4.73	4.65	4.57
	10	10.0	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.94	4.85	4.71	4.56	4.41	4.33	4.25	4.17
	11	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74	4.63	4.54	4.40	4.25	4.10	4.02	3.94	3.86
	12	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.50	4.39	4.30	4.16	4.01	3.86	3.78	3.70	3.62
	13	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.19	4.10	3.96	3.82	3.66	3.59	3.51	3.43
	14	8.86	6.51	5.56	5.04	4.69	4.46	4.28	4.14	4.03	3.94	3.80	3.66	3.51	3.43	3.35	3.27
	15	8.68	6.36	5.42	4.89	4.56	4.32	4.14	4.00	3.89	3.80	3.67	3.52	3.37	3.29	3.21	3.13
	16	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.78	3.69	3.55	3.41	3.26	3.18	3.10	3.02
	17	8.40	6.11	5.18	4.67	4.34	4.10	3.93	3.79	3.68	3.59	3.46	3.31	3.16	3.08	3.00	2.92
	18	8.29	6.01	5.09	4.58	4.25	4.01	3.84	3.71	3.60	3.51	3.37	3.23	3.08	3.00	2.92	2.84
	19	8.18	5.93	5.01	4.50	4.17	3.94	3.77	3.63	3.52	3.43	3.30	3.15	3.00	2.92	2.84	2.76
	20	8.10	5.85	4.94	4.43	4.10	3.87	3.70	3.56	3.46	3.37	3.23	3.09	2.94	2.86	2.78	2.69
	21	8.02	5.78	4.87	4.37	4.04	3.81	3.64	3.51	3.40	3.31	3.17	3.03	2.88	2.80	2.72	2.64
	22	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35	3.26	3.12	2.98	2.83	2.75	2.67	2.58
	23	7.88	5.66	4.76	4.26	3.94	3.71	3.54	3.41	3.30	3.21	3.07	2.93	2.78	2.70	2.62	2.54
	24	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26	3.17	3.03	2.89	2.74	2.66	2.58	2.49
	25	7.77	5.57	4.68	4.18	3.85	3.63	3.46	3.32	3.22	3.13	2.99	2.85	2.70	2.62	2.54	2.45
	30	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07	2.98	2.84	2.70	2.55	2.47	2.39	2.30
	40	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89	2.80	2.66	2.52	2.37	2.29	2.20	2.11
	60	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72	2.63	2.50	2.35	2.20	2.12	2.03	1.94
	120	6.85	4.79	3.95	3.48	3.17	2.96	2.79	2.66	2.56	2.47	2.34	2.19	2.03	1.95	1.86	1.76
	∞	6.63	4.61	3.78	3.32	3.02	2.80	2.64	2.51	2.41	2.32	2.18	2.04	1.88	1.79	1.70	1.59

B.6A Critical Values of the F Distribution ($\alpha = .05$)



		Degrees of Freedom for the Numerator															
		1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40
Degrees of Freedom for the Denominator	1	161	200	216	225	230	234	237	239	241	242	244	246	248	249	250	251
	2	18.5	19.0	19.2	19.2	19.3	19.3	19.4	19.4	19.4	19.4	19.4	19.4	19.4	19.5	19.5	19.5
	3	10.1	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.70	8.66	8.64	8.62	8.59
	4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.91	5.86	5.80	5.77	5.75	5.72
	5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.68	4.62	4.56	4.53	4.50	4.46
	6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.94	3.87	3.84	3.81	3.77
	7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.51	3.44	3.41	3.38	3.34
	8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.28	3.22	3.15	3.12	3.08	3.04
	9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.01	2.94	2.90	2.86	2.83
	10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.91	2.85	2.77	2.74	2.70	2.66
	11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.79	2.72	2.65	2.61	2.57	2.53
	12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.69	2.62	2.54	2.51	2.47	2.43
	13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.60	2.53	2.46	2.42	2.38	2.34
	14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.53	2.46	2.39	2.35	2.31	2.27
	15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54	2.48	2.40	2.33	2.29	2.25	2.20
	16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49	2.42	2.35	2.28	2.24	2.19	2.15
	17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.38	2.31	2.23	2.19	2.15	2.10
	18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41	2.34	2.27	2.19	2.15	2.11	2.06
	19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.31	2.23	2.16	2.11	2.07	2.03
	20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.28	2.20	2.12	2.08	2.04	1.99
	21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.25	2.18	2.10	2.05	2.01	1.96
	22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.23	2.15	2.07	2.03	1.98	1.94
	23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.20	2.13	2.05	2.01	1.96	1.91
	24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.11	2.03	1.98	1.94	1.89
	25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.16	2.09	2.01	1.96	1.92	1.87
	30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.09	2.01	1.93	1.89	1.84	1.79
	40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.00	1.92	1.84	1.79	1.74	1.69
	60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.92	1.84	1.75	1.70	1.65	1.59
	120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.96	1.91	1.83	1.75	1.66	1.61	1.55	1.50
	∞	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.88	1.83	1.75	1.67	1.57	1.52	1.46	1.39