



**SET A**

---

**UNIVERSITI KUALA LUMPUR  
Malaysia France Institute**

---

**FINAL EXAMINATION  
JANUARY 2014 SESSION**

---

**SUBJECT CODE : FAD 30203**  
**SUBJECT TITLE : CONTROL ENGINEERING**  
**LEVEL : DIPLOMA**  
**TIME / DURATION : (3 HOURS)**  
**DATE :**

---

**INSTRUCTIONS TO CANDIDATES**

---

- 1. Please read the instructions given in the question paper CAREFULLY.**
- 2. This question paper is printed on both sides of the paper.**
- 3. Please write your answers on the answer booklet provided.**
- 4. Answer should be written in blue or black ink except for sketching, graphic and illustration.**
- 5. This question paper consists of TWO (2) sections. Section A and B. Answer all questions in Section A. For Section B, answer TWO (2) questions only.**
- 6. Answer all questions in English.**
- 7. Semi-log paper and formula is appended**

---

**THERE ARE 6 PAGES OF QUESTIONS AND 3 PAGES OF APPENDICES, EXCLUDING THIS PAGE.**

---

**SECTION A (Total: 60 marks)**

**INSTRUCTION: Answer all the questions.**  
**Please use the answer booklet provided.**

**Question 1**

- (a) A Segway® Personal Transporter (PT) is a two wheeled vehicle in which human act as operator stands vertically on a platform. As the driver leans left, right, forward and backward, a set of sensitive gyroscopic sensors sense the desired input. These signals are fed to a computer that amplifies them and commands motors to propel the vehicle in the desired direction. Determine whether the system is an open-loop or a closed-loop control system and provide your justification.

(4 marks)



**Figure 1:** The Segway® Personal Transporter (PT)

- (b) Consider the human is trying to reach for a book in the table. Determine the reference input and the controller of the task.

(2 marks)

- (c) Describe how does an open-loop system differs from closed-loop systems. List **one (1)** advantage of each system.

(4 marks)

- (d) Find the forward Laplace for: (4 marks)

i.  $5 \frac{d^2 y(t)}{dt^2} + 8 \frac{dy(t)}{dt} + 3y(t)$ .

ii.  $\frac{t^{6-1} e^{-2t}}{6-1!}$ .

- (e) Find the inverse Laplace for  $\frac{8}{s(s^2 + 5s + 6)}$ . (6 marks)

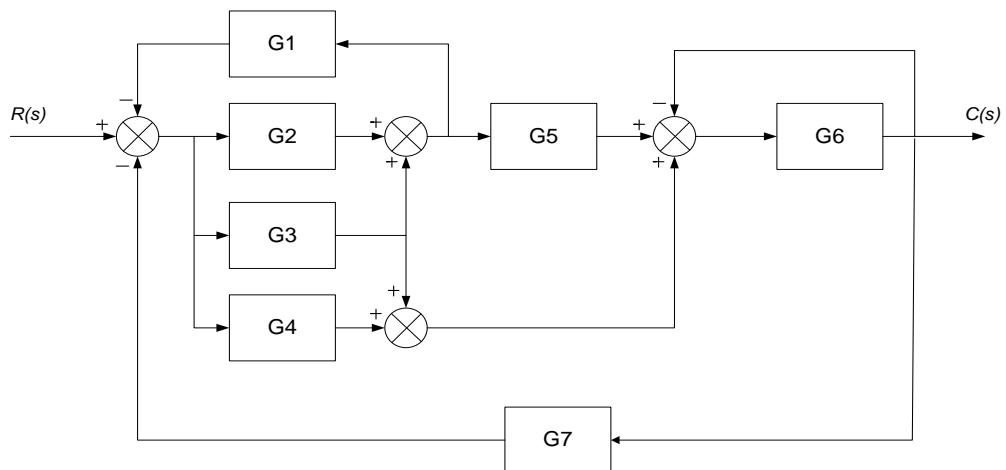
**Question 2**

- (a) Prove that for a positive-feedback closed-loop control system, the system transfer function is  $TF = \frac{G}{1 - GH}$ , where **G** is forward gain and **H** is feedback gain.

(5 marks)

- (b) Simplify the block diagram of a system shown in **Figure 2** to a single block representing the transfer function,  $TF(s) = \frac{C(s)}{R(s)}$ .

(12 marks)



**Figure 2:** Block Diagram

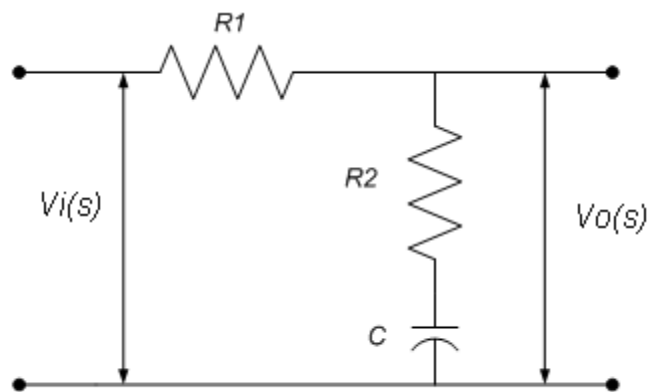
- (b) Obtain the transfer function,  $TF(s)$  if  $G_1(s)=1$ ,  $G_2(s)=2$ ,  $G_3(s)=4$ ,  $G_4(s)=2$ ,  $G_5(s)=1$ ,  $G_6(s)=2$  and  $G_7(s)=1$ .

(3 marks)

**Question 3**

- (a) Define mathematical modeling. (2 marks)
- (b) Determine the transfer function of the circuit in **Figure 3** for output voltage  $V_o(s)$ , versus input voltage  $V_i(s)$ . Output voltage is measured across the  $R_2$  and  $C$ .

(10 marks)

**Figure 3:** Series RC circuit

- (c) A basic mechanical system consist of three passive and linear components; mass, spring and viscous damper. Derive the **mathematical model** that describe the relationship between force  $f(t)$  and displacement  $x(t)$  for each components. (6 marks)
- (d) Provide an example of mechanical system that you know. (2 marks)

(2 marks)

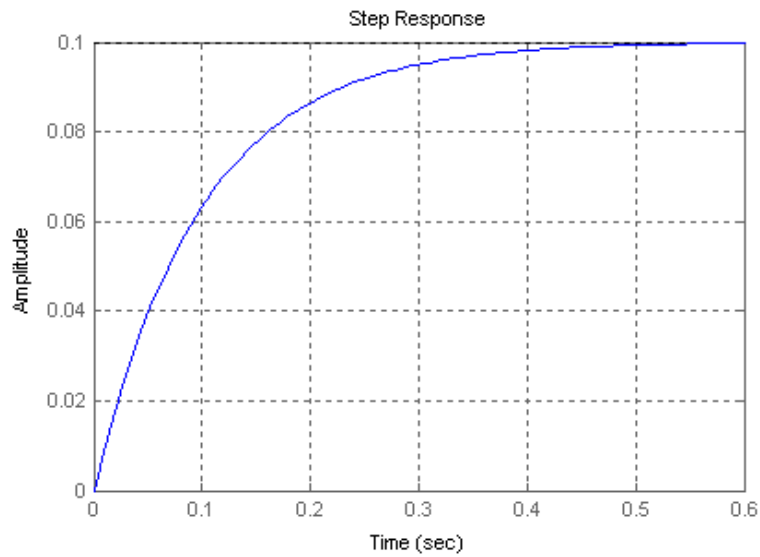
**SECTION B (Total: 40 marks)**

**INSTRUCTION: Answer TWO (2) questions only.**

**Please use the answer booklet provided.**

**Question 4**

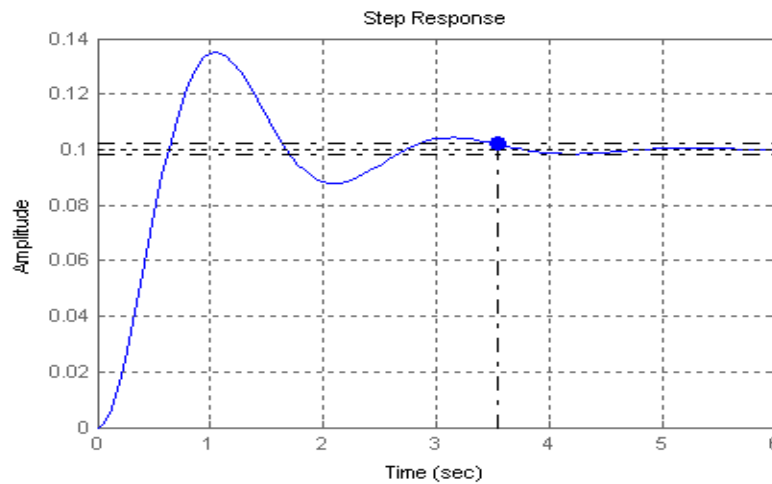
- (a) Find the transfer function for the unit step response of the first order response below. (10 marks)



**Figure 4: First Order response**

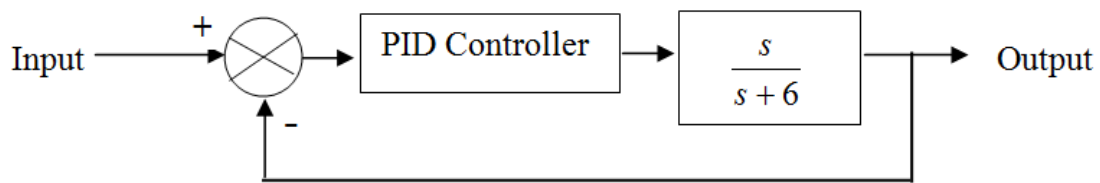
- (b) Given that the settling times ( $T_s$ ) of the second order response below is 3.54s and find the transfer function of the system.

(10 marks)



**Figure 5: Second Order response**

**Question 5**

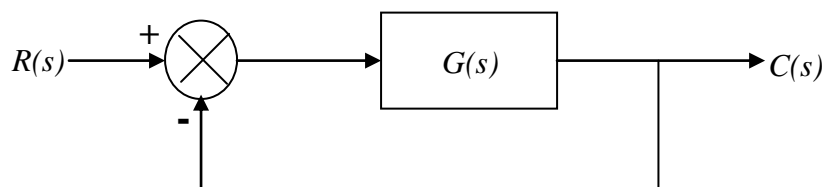


**Figure 6:** PID controller with plant module system

- (a) Define and give an application of PID controller. (4 marks)
- (b) Find the transfer function of PID controller. (5 marks)
- (c) Based on **Figure 6** find the transfer function when PID controller connected in series with the plant module. (5 marks)
- (d) Give the characteristic of P, I and D controller. (6 marks)

**Question 6**

- (a) Draw a Bode plot of the unity feedback system shown in **Figure 7**. (14 marks)



**Figure 7:** The unity feedback system

Where 
$$G(s) = \frac{60}{s(s+5)(s+12)}$$

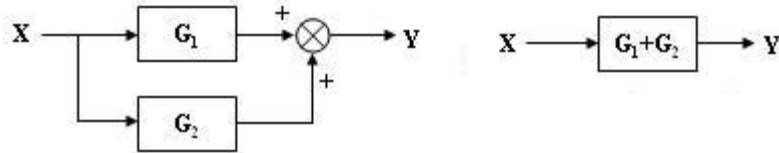
- (b) From the Bode plot, determine the following:
- i. Gain margin,  $GM$  (1 mark)
  - ii. Phase margin,  $PM$  (1 mark)
  - iii. Gain cross over frequency,  $\omega_{gco}$  (1 mark)
  - iv. Phase cross over frequency,  $\omega_{pco}$  (1 mark)
- (c) Give your comment on the stability. (2 marks)

**END OF QUESTION**

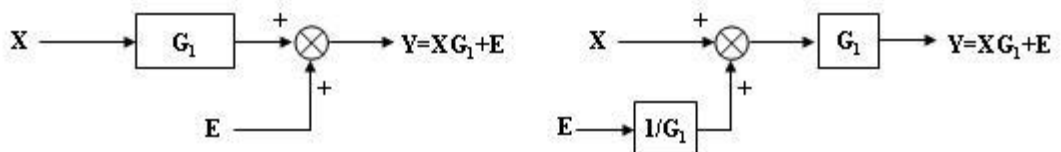
**1. Cascading Blocks:**



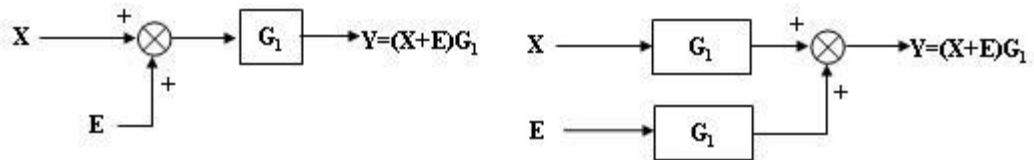
**2. Blocks in parallel: Forward Loop**



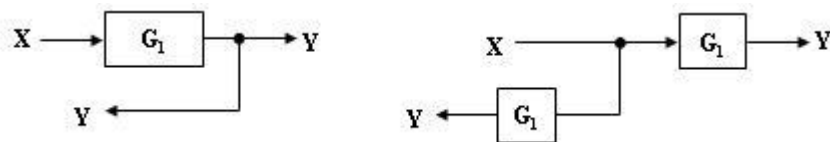
**3. Moving the summing ahead of the block:**



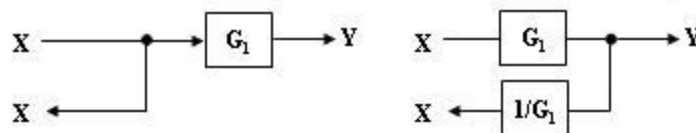
**4. Moving the summing beyond the block:**



**5. Moving the takeoff point ahead of a block:**



**6. Moving the takeoff point beyond a block:**





APPENDIX 2: TABLE OF LAPLACE TRANSFORMS

	Time domain $f(t)$	Laplace domain $F(s)$
1	Unit impulse $\delta(t)$	1
2	Unit Step Function $u(t)$	$\frac{1}{s}$
3	Constant $K$	$\frac{K}{s}$
4	$t$	$\frac{1}{s^2}$
5	$t^2$	$\frac{2!}{s^3}$
6	$\frac{t^2}{2!}$	$\frac{1}{s^3}$
7	$t^n$	$\frac{n!}{s^{n+1}}$
8	$\frac{t^{n-1}}{n!}$	$\frac{1}{s^n}$
9	$e^{-at}$	$\frac{1}{s+a}$
10	$t \cdot e^{-at}$	$\frac{1}{(s+a)^2}$
11	$\frac{t^2 e^{-at}}{2!}$	$\frac{1}{(s+a)^3}$
12	$\frac{t^{n-1} e^{-at}}{n-1!}$	$\frac{1}{(s+a)^n}$
13	$\sin \omega t$	$\frac{\omega}{s^2 + \omega^2}$
14	$\cos \omega t$	$\frac{s}{s^2 + \omega^2}$
15	$\frac{1}{a}(1 - e^{-at})$	$\frac{1}{s(s+a)}$
16	$\frac{1}{a^2}(at - 1 + e^{-at})$	$\frac{1}{s^2(s+a)}$
17	$\frac{1}{b-a}(e^{-at} - e^{-bt})$	$\frac{1}{(s+b)(s+a)}$
18	$e^{-at} \sin \omega t$	$\frac{\omega}{(s+a)^2 + \omega^2}$
19	$e^{-at} \cos \omega t$	$\frac{s+a}{(s+a)^2 + \omega^2}$

## APPENDIX 3: FORMULAS

1	$T_s \approx 4T = \frac{4}{\xi\omega_n}, \text{ if 2\% of final value}$ $T_s \approx 3T = \frac{3}{\xi\omega_n}, \text{ if 5\% of final value}$
2	$\%OS = \frac{c_{\max} - c_{\text{final}}}{c_{\text{final}}} \times 100$
3	$\xi = \frac{-\ln(\%OS/100)}{\sqrt{\pi^2 + \ln^2(\%OS/100)}}$
4	$T_p = \frac{\pi}{\omega_n \sqrt{1 - \xi^2}}$